CMPS 12B
Introduction to Data Structures
Final Review Problems

Study the review problems from the previous midterms, along with the midterm solutions.

1. The keys 28, 5, 15, 19, 10, 17, 33, 12, 20, 6, 9, 23, 34, 22 and 21 are to be inserted in order into a hash table of length 9.

   a. Suppose that collisions are to be resolved by chaining, with insertions performed at the head of each list. The hash function is \( h(k) = k \mod 9 \). Show the state of the hash table after all insertions are performed, i.e. draw the array and the linked lists which result.

   b. Referring to part (a), what is the load factor \( \alpha \)? How many collisions are there?

   c. Show the result of inserting the same keys into a hash table of length 9 where collisions are resolved by open addressing, with hash function: \( h(k, i) = (k \mod 9 + 5i) \mod 9 \). Note that in this case there are more keys than slots, so you won’t be able to insert all the keys. Just insert the keys in the given order until there is no more room in the table. Again draw a picture of the array and its contents.

2. Fill in the definition of the C function below called printPreOrder(). This function will, given the root \( N \) of a binary search tree based on the Node structure below, print out the keys according to a pre-order tree traversal. Write similar functions called printInOrder() and printPostOrder() that print in-order and post-order tree traversals respectively.

```c
typedef struct Node{
    int key;
    struct Node* left;
    struct Node* right;
} Node;

typedef Node* NodeRef;

void printPreOrder(NodeRef N){

}
```
3. Draw the Binary Search Tree resulting from inserting the keys: 5 8 3 4 6 1 9 2 7 (in that order) into an initially empty tree. Draw another BST that results from deleting the keys 5 1 7 (in that order) from the previous tree. Show the output of functions printInOrder(), printPreOrder() and printPostOrder() from problem 2 when run on the root of this tree.

4. The public class Node defined below can be used to build a binary search tree in java. Trace the main function in the class problem3 below and draw the binary search tree that results. Write java instructions which will "manually" perform the following operations in succession: insert the key 1, insert the key 3, delete the key 7. Draw the resulting binary search tree.

```java
// Node.java
public class Node{
    int key;
    Node left;
    Node right;

    Node(int k){
        this.key = k;
        this.left = this.right = null;
    }
}

// problem4.java
public class problem4{
    public static void main(String[] args){
        Node root = new Node(5);
        root.left = new Node(2);
        root.right = new Node(7);
        root.right.left = new Node(4);
        root.right.right = new Node(8);
        // your code goes here
    }
}
```
5. Write a C function with prototype `char* cat(char* s1, char* s2)` that takes two null terminated char arrays `s1` and `s2`, allocates sufficient heap memory to store the concatenation of the two arrays (including a terminating null character), copies the contents of arrays `s1` and `s2` into that newly allocated array (including the terminating null character), then returns a pointer to the new char array. You may not use functions from the `string.h` library to accomplish the above tasks, in particular, you must manually determine the length of char arrays `s1` and `s2` by searching for their terminating null characters.

6. Write a Java function with the heading `void sortWords(String[] W)` that sorts its array argument `W` in alphabetical order. Do this by implementing the Insertion Sort algorithm discussed in class.

7. Re-do problem 6 but this time in C. Use the function heading `void sortWords(char** W, int n)`. Assume that `W` is an array of length `n` whose elements are null-terminated char arrays (i.e. C strings).