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①

## What to know for Quiz 4

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\* <sup>ever</sup> anything on Quiz 1.

\* recite the robot model from memory

\* Given the wall-following control

Control Law 
$$\begin{cases} u_k = u_{nom} \\ v_k = k_p(x_k - d_{sep}) + k_d \left( \frac{x_k - x_{k-1}}{\Delta} \right) \end{cases}$$

Compute the fixed-point(s) for the  $(x, \theta)$  dynamics

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$$x_{k+1} = x_k + \Delta u_k \cos(\theta_k)$$

$$\theta_{k+1} = \theta_k + \Delta v_k$$

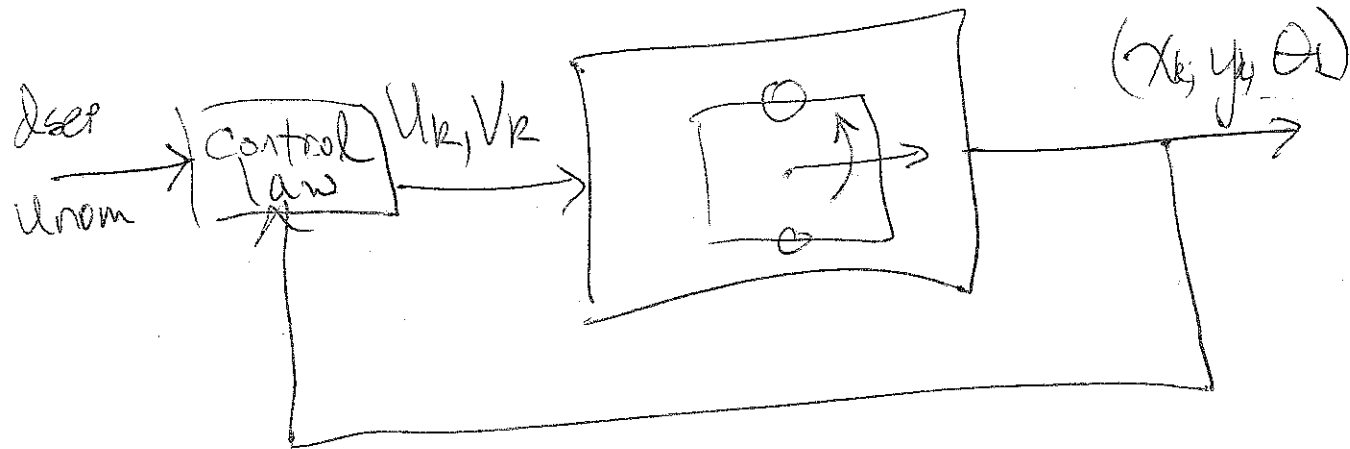
Substitute  $\rightarrow$

$$\begin{cases} x_{k+1} = x_k + \Delta u_{nom} \cos(\theta_k) \\ \theta_{k+1} = \theta_k + \Delta \left[ k_p(x_k - d_{sep}) + \left( \frac{x_k - x_{k-1}}{\Delta} \right) k_d \right] \end{cases}$$

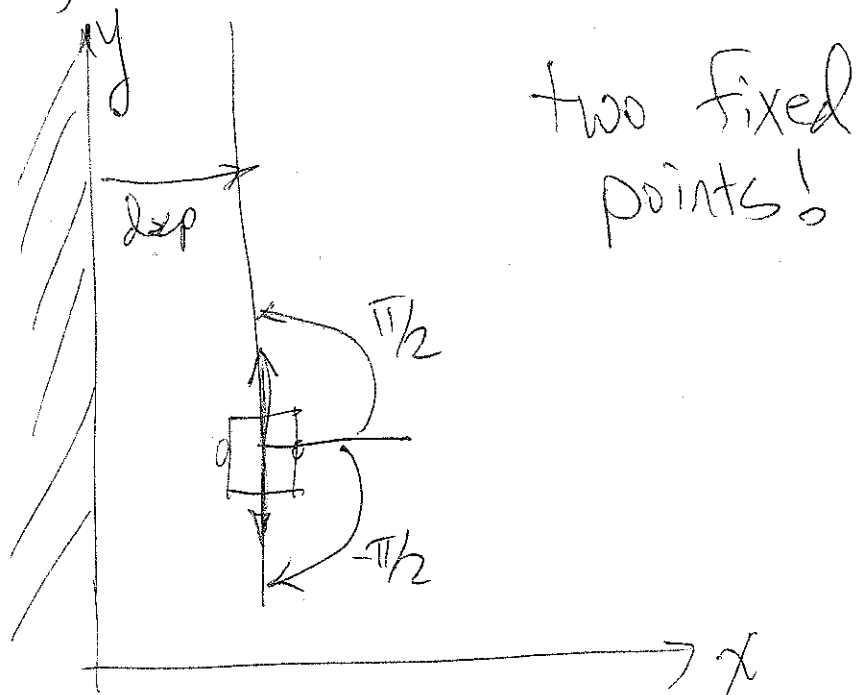
the closed-loop dynamics

Aside

Block Diagram



Show that for the closed-loop dynamics,  $(x_*, \theta_*) = (d_{sep}, \pm \pi/2)$



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closed-loop  $y$ -dynamics

at  $\Theta_k = \Theta_* = \pm \pi/2$

$$\underline{y_{k+1} = y_k + \Delta(\pm 1 * u_{nom})}$$