

HYPOTHESIS TEST (Continued)

We must compare $\bar{y} \stackrel{!}{=} \mu_0$ with respect to the noisiness (uncertainty) of \bar{y} .

$$(* = \bar{y} = 25.0^\circ\text{C}) \text{ vs. } (** = \mu_0 = 24.3^\circ\text{C})$$

We assume that the null is true ($\mu = 24.3 = \mu_0$) and do a T-Test:

T-Test:
$$\frac{\bar{y} - \mu_0}{(SE_{\text{IID}}(\bar{y}) \text{ if null is true})} = \frac{\bar{y} - \mu_0}{(s/\sqrt{n})}$$

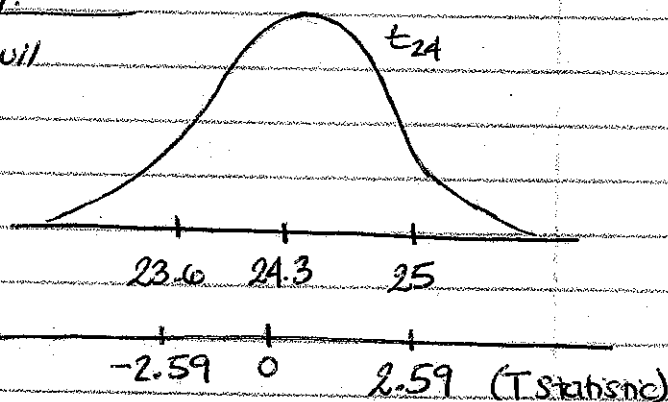
T-Test for crab body $T^\circ\text{C}$.

$$\frac{\bar{y} - \mu_0}{(s/\sqrt{n})} = \frac{25^\circ\text{C} - 24.3^\circ\text{C}}{(0.27)} = \boxed{\frac{\text{signal}}{\text{noise}}} = 2.59 = t$$

2.59 = T-STATISTIC

meaning: μ_0 is about $2\frac{1}{2}$ standard errors away from \bar{y} .

Long Run Histogram if null true, accounting for uncertainty in σ



What is the chance of getting data this extreme?

NUMERICAL SURPRISE MEASURE \hookrightarrow P Value \rightarrow The Area to the Right of your T statistic

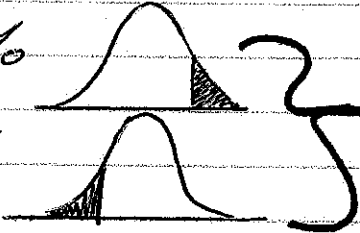
As $T \uparrow$, $P \downarrow$

- a larger P value means that the data is not as surprising (high chance of getting such data).

THE DIFFERENT ALTERNATIVES:

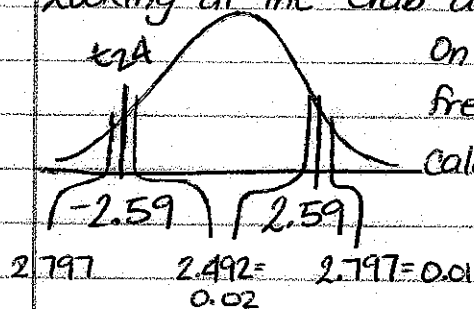
Alternative 1: $\mu \neq \mu_0$ \longrightarrow 2-sided alternative
 2-tailed P-value
 (2-tailed test)

Alternative 2: $\mu > \mu_0$
 Alternative 3: $\mu < \mu_0$



\longrightarrow 1-sided alternative
 1-tailed P-value
 (1-tailed test)

Looking at the crab data:



On T-Table, look at 24 degrees of freedom, and find where the calculated p. value fits

- Our particular p value of 2.59 is not on the T-table, but it is somewhere between the values of

$\frac{2.797}{0.01}$ & $\frac{2.492}{0.02}$

Area in 2 Tails:

Our p-value is between 1% & 2% = small
 Small p value \rightarrow reject

We appeal to conventional values to decide if p is small is small enough to reject null & favor the alternative.

$P \leq 5\%$, reject null: result = STATSIG

$P \leq 1\%$, result = highly STATSIG

We estimated our P-value to be between 1% & 2%.

We can use JMP to get a finer value:

2.59 \rightarrow 1.6% (STATSIG, but not highly STATSIG)

When hypothesis testing is done with a 2-sided alternative, its conclusion is identical to the CI approach.

PITFALLS OF HYPOTHESIS TESTING

- 1) more complicated, more vocabulary, not as transparent as CI.
- 2) Usually hypothesis testing is done the opposite way:
 - null = theory is wrong
 - alternative = theory is right
 because it is easier to manipulate the P value. Most scientific journals want $P \leq 5\%$, so if your 2-tailed P-value is too big, you can just cut it in half and publish with a 1-tailed P-value.

 $1\text{-tailed } p = 4\% \quad \equiv \quad 2\text{-tailed } p = 8\%$

 Rigid adherence to $p \leq 5\%$ is silly.
- 3) For a 2-tailed P-value, you cannot tell if \bar{y} is above or below μ_0 (cannot reconstruct \bar{y} from the result, or anything else for that matter).
- 4) It is useful to know how big the signal ($\bar{y} - \mu_0$) and the noise (S/\sqrt{n}) are, but if you get:

$$\frac{\text{signal}}{\text{noise}} = 0.5$$
 you don't know if 0.5 stands for $\frac{1}{2}$ or $\frac{2}{4}$, and because of this (once again) you can't reconstruct \bar{y} .
 - With CI you can back-calculate to find out what the original #'s were
 - ex: \bar{y} is right in the middle of the interval.
- 5) For every new theoretical μ_0 , you need to build a new hypothesis test (you can reuse same CI).

GENERALLY A GOOD WAY TO MEASURE PRACTICAL SIGNIFICANCE:

Compute the difference between \bar{y} & μ_0 in relation to μ_0

\bar{y} = treatment

μ_0 = control

$$100 \left(\frac{T-C}{C} \right) \% \quad \left[\geq 5\% = \text{practsig} \right]$$

The relative difference on an order of 5% or more tends to be large in practical terms (practsig)

EXAMPLE: Does Calcium concentration in an arthropod species match the Calcium concentration ($[Ca^{2+}]$) in the water?

$[Ca^{2+}]$ of water = 32 mmole/kg

Sample size $n = 4$ arthropods

$\bar{y} [Ca^{2+}] = 29.8$ mmole/kg

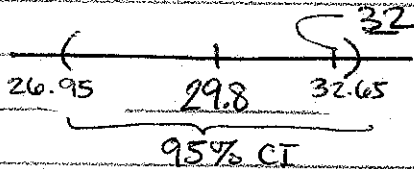
$S = 1.79$ mmole/kg

PRACTICALLY SIGNIFICANT?

$$100 \left(\frac{T-C}{C} \right) \% = 100 \left(\frac{29.8 - 32}{32} \right) \% = 6.9\% \quad \text{PRACTSIG}$$

STATSIG?

build a 95% CI for $\mu = \bar{y} \pm (t_{3}^{0.95})(S/\sqrt{n})$
 $= 29.8 \pm (3.182)(1.79/\sqrt{4}) = 26.95 \text{ } \overset{32}{\underset{32.65}{}}$



32 does fit in the 95% CI

NOT STAT SIG

NOT ENOUGH DATA: Practsig, not Statsig

The SE is too big

TOO MUCH DATA: not Practsig, ^{yes} Statsig

The SE is too small

How many arthropods need to be collected for practical significance & statistical significance to be in focus?

Build a 95% CI w/ n observations

$$95\% \text{ CI} = 100(1-\alpha)\% \rightarrow \boxed{\alpha = 0.05}$$

$$\bar{y} \pm (t_{n-1}^{0.95(2)}) (s/\sqrt{n})$$

→ area in 2 tails combined must be 5%

This is a pre-experiment calculation

- You need to have some past experience in a similar experiment to have a vague idea of where to start.

° Suppose past experience makes you think $s = 1.8$.

Somebody told you a $[\text{Ca}^{2+}]$ of 31.5 in an arthropod is a lot different from a $[\text{Ca}^{2+}] = 32$.

CI will discriminate between 2 theories:

$$\mu_0 = 32 \text{ mmol/kg}$$

$$\mu_A = 31.5 \text{ mmol/kg}$$

IF μ_0 falls just outside the 95% CI:

$$\mu_0 = \mu_A + (t_{n-1}^{0.95(2)}) (s/\sqrt{n}) \rightarrow \text{SOLVE FOR } n$$

$$n = \frac{(t_{n-1}^{(1-\alpha)/2})^2 (s)^2}{(\mu_0 - \mu_A)^2}$$

Problem: T depends on n
 $n \rightarrow n$ technically on both sides of equation

Equation must be solved iteratively

such that your initial guess for $n = \infty$

$n = \infty \rightarrow$ follows normal curve

$t = Z = 1.96$ for 95% certainty

* you can trick JMP into doing iterations for you.

SAMPLE SIZE DETERMINATION

ARTHROPODS \rightarrow how many?

$$S = 1.8 \text{ mmol/kg}$$

$$(M_0 - M_A) = (32 - 31.5) = 0.5 \text{ mmol/kg}$$

$$n = \frac{(t_{n-1}^{(1-\alpha)2})^2 (S)^2}{(M_0 - M_A)^2} \quad n_i = \infty$$

$$\infty = \frac{(1.96)^2 (1.8)^2}{(0.5)^2} = 49.8 = 50 = n$$

In Table, $n-1 \rightarrow$ 49 degrees of freedom \Rightarrow 2.009

$$50 = \frac{(2.009)^2 (1.8)^2}{(0.5)^2} = 52.3 \approx 53 = n$$

52 \rightarrow 2.008

$$53 = \frac{(2.008)^2 (1.8)^2}{(0.5)^2} = 52.3 \approx 53$$

53 is repeated \rightarrow $n=53$

Our sample size should be about 53 arthropods to be sure that our practical significance and statistical significance are focused in relation to each other.