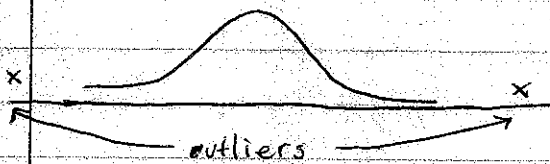


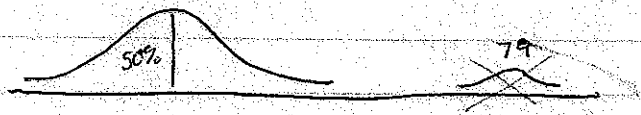
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Outliers: Sensitivity Analysis



data values that are far from the bulk of the data

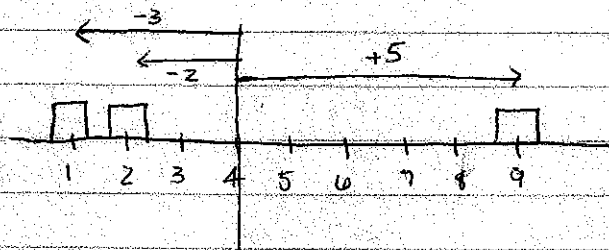
- Means are very sensitive to outliers
- The median, however, is not affected by outliers



Measures of Spread

- 1
- 2
- 9

$\bar{y} = 4$



- 1
- 2
- 9

subtract
 \bar{y}

- 1 - 4 = -3
- 2 - 4 = -2
- 9 - 4 = 5

deviations from the mean

- y_1
- y_2
- y_3

subtract
 \bar{y}

- $y_1 - \bar{y}$
- $y_2 - \bar{y}$
- $y_3 - \bar{y}$

- Need to get rid of cancellation of + and - signs
- idea 1: use absolute values

$$\begin{bmatrix} |y_1 - \bar{y}| \\ \vdots \\ |y_n - \bar{y}| \end{bmatrix} = \begin{bmatrix} |1-4| \\ |2-4| \\ |9-4| \end{bmatrix} = \begin{bmatrix} 3 \\ 2 \\ 5 \end{bmatrix} \quad \text{mean} = \frac{10}{3} = 3.3$$

Mean Absolute Deviation (MAD)
(not used much)

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- idea 2: square the deviations

$$\begin{bmatrix} (y_1 - \bar{y})^2 \\ (y_2 - \bar{y})^2 \\ (y_3 - \bar{y})^2 \end{bmatrix} = \begin{bmatrix} -3^2 \\ -2^2 \\ 5^2 \end{bmatrix} = \begin{bmatrix} 9 \\ 4 \\ 25 \end{bmatrix}$$

mean = $\sqrt{12.7}$

- Standard Deviation (SD)

$$\sqrt{\frac{(y_1 - \bar{y})^2 + (y_2 - \bar{y})^2 + \dots + (y_n - \bar{y})^2}{n-1}}$$

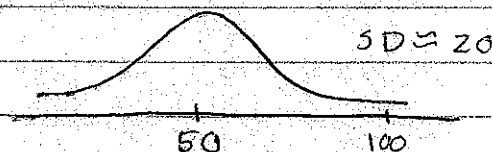
$$s = \sqrt{\frac{(y_1 - \bar{y})^2 + \dots + (y_n - \bar{y})^2}{n-1}} = \sqrt{\frac{1}{n-1} \sum_{i=1}^n (y_i - \bar{y})^2}$$

• Why divide by $n-1$ instead of n ?

$\begin{bmatrix} 1 \\ 2 \\ 9 \end{bmatrix}$ $\begin{bmatrix} \checkmark \\ \checkmark \\ X \end{bmatrix}$ \rangle 1st 2 free to vary
 mean = 4 mean = 4 A data set has only $n-1$ degrees of freedom for measuring spread

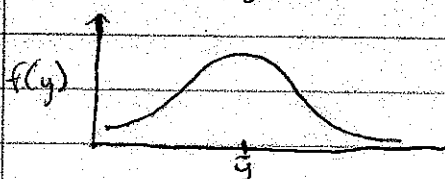
- Graphical Interpretation of SD

$$s = \sqrt{\frac{1}{n-1} \sum_{i=1}^n (y_i - \bar{y})^2}$$



* each # in this data set is around 50, give or take around 20

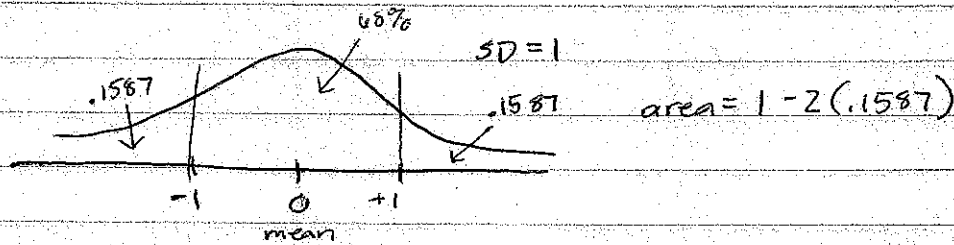
1.4: Using the Normal Distribution Descriptively



$$f(y) = \frac{1}{\sigma\sqrt{2\pi}} e^{-\frac{(y-\bar{y})^2}{2\sigma^2}}$$

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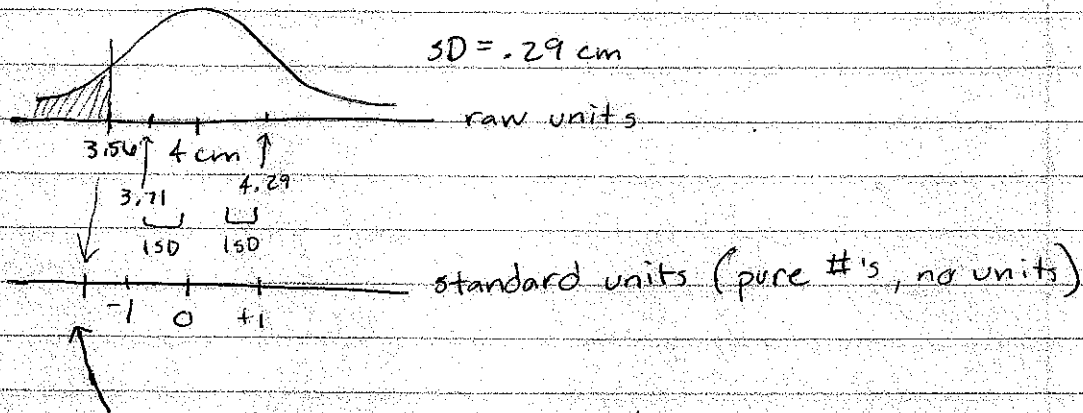
Standard Normal Curve



Facts about Normal Curve

- 1) symmetric
- 2) total area under it is 1

Butterfly Wing Length



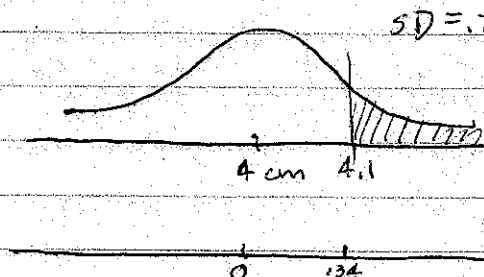
convert 3.56 to standard units

$$\frac{3.56 - 4.0 \text{ cm}}{.29 \text{ cm}} = -1.52$$

- use table to find area: = .0643 = 6.4%
- actual answer = 8.3%

* normal approximation here is good, but not great

Example:



What % of data is above 4.1 cm?

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$$\frac{4.1 - 4.0 \text{ cm}}{.29 \text{ cm}} = \frac{.1}{.29} = .34$$

• area using standard table = .3669 = 36.7% \approx 37%

• actual % = 38%

- General formula for converting to standard units:

$$\frac{\# - \text{mean}}{SD} = z = \frac{y - \bar{y}}{s}$$